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## Spontaneous Transition Probabilities and Branching Ratios for the Excited States of Pr<sup>3+</sup> in Acetylacetonate

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UV-VIS absorption spectrum of  $Pr^{3+}$  in acetylacetonate chelate dissolved in five solvents, viz. (a) methanol, (b) ethanol, (c) DMF, (d) methanol + ethanol (1:3) and (e) DMF + solvent (d) (1:4) were recorded. From the observed spectral intensities of the bands, the three phenomenological Judd Ofelt parameters  $\Omega_2$ ,  $\Omega_4$  and  $\Omega_6$  have been evaluated. Radiative transition probabilities (A), radiative relaxation rates ( $A_T$ ), radiative lifetimes ( $T_R$ ) and branching ratios ( $\beta_R$ ) for the excited  ${}^{3}P_1$ ,  ${}^{3}P_0$  and  ${}^{1}D_2$  levels were calculated and their usefulness for laser action is discussed.

Key Words: Radiative lifetimes, laser action, Judd-Ofelt parameters.

#### INTRODUCTION

In view of the potential laser action of rare earth chelates, many researchers<sup>1-10</sup> studied them in different organic solvents. The present paper reports the calculated radiative transition probabilities and branching ratios for the excited fluorescent levels of  $Pr^{3+}$  in acetyl-acetonate dissolved in certain organic solvents from the observed spectral intensities of the bands.

#### **EXPERIMENTAL**

#### **Preparation of RE Chelates**

Freeman and Crosby<sup>11</sup> reported details of the preparation of trisacetylacetonate chelates. Approximately 2g of praseodymium chloride (99.99%) was dissolved in 200 ml of distilled water. To this, 8 ml of redistilled acetylacetone was added. Concentrated ammonium hydroxide was added to this mixture drop by drop with vigorous stirring until precipitation of white microcrystalline chelate was complete. The precipitated chelate was collected by suction on a medium sintered glass filter funnel, washed with distilled water, air dried at room temperature and recrystallized from boiling acetone. Finally the recrystallized chelate was vacuum dried at room temperature for about 16 hours.

#### SPECTROSCOPIC MEASUREMENTS

For absorption measurements, the praseodymium acetylacetonate thus prepared was dissolved in five different solvents (a) methanol (MA), (b) ethanol (EA), (c) dimethyl formamide (DMF), (d) MA + EA (1:3) and (e) mixture of (c) and (d) by 4:1 in volume. All the solutions were prepared with a chelate concentration of 0.01 M just before its use.

Absorption spectra of five solutions were recorded in the wavelength region 400 to 620 nm on a Perkin-Elmer 551 spectrophotometer. Refractive indices (n) of these solutions were measured at different wavelengths of mercury by minimum deviation method using hallow glass prism and a spectrometer. The variation of refractive index (n) with wavelength ( $\lambda$  in Å) could be fitted to the following formula in the case of the chelates studied<sup>12</sup>

$$n = 1.3124 + \frac{81.9124}{\lambda(\text{\AA}) - 744.023} \tag{1}$$

The spectral intensities were determined by measuring the area under the absorption curves using the weight method. The oscillator strengths of the bands were calculated using the relation

$$f_{\text{expt}} = 4.32 \times 10^{-9} \int \varepsilon(v) \, dv \tag{2}$$

where  $\varepsilon(v)$  is the molar extinction coefficient at wavenumber v.

#### RESULTS AND ANALYSIS

#### **Energy Levels**

UV-VIS absorption spectra recorded for  $Pr^{3+}$  in acetylacetonate chelate complex in the five different organic solvents are shown in Figure 1. Only four bands could be observed in all the complexes studied. They are  ${}^{1}D_{2}$ ,  ${}^{3}P_{0}$ ,  ${}^{3}P_{1}$  and  ${}^{3}P_{2}$ . The energy levels of lanthanides arise due to the electrostatic and spin-orbit interactions between the  $4f^{n}$  electrons. Since in the present work, only four bands are observed,  $F_{4}$  and  $F_{6}$  parameters are fixed in terms of  $F_{2}$  assuming radial wavefunctions to be hydrogenic and using the following expressions<sup>13</sup>

$$F_4 = 0.138 F_2$$
  
 $F_6 = 0.0151 F_2$ 

Introducing these Slater-Condon  $(F_k)$  parameters in Racah  $(E^k)$  parameters we obtain

$$E^1 = 14.68 F_2$$
  
 $E^2 = 0.077 F_2$ 



Figure 1 Absorption spectra of  $Pr^{3+}$  in Acetyl Acetonate in different organic solvents.

and

$$E^3 = 1.48 F_2$$

From the expressions of Dieke<sup>13</sup>

$$F_2 = 12.4 (Z - 34)$$

where Z = 59 for praseodymium, the value of  $F_2$  is first evaluated and thus  $E^1$ ,  $E^2$  and  $E^3$  are calculated. The  $f^2$  configuration energy matrices<sup>14</sup> are solved with these  $E^1$ ,  $E^2$  and  $E^3$  and aquo ion  $\xi$  value of 750 cm<sup>-1</sup>. The matrices are again solved with the same  $E^k$  but  $\xi = 751$  cm<sup>-1</sup>. The difference of the latter and former values gives the partial derivative  $dE/d\xi$  for each state. The energy of the state in the former case is  $E_{0J}$  (zero order energy). These values are given in Table 1. Substituting the observed band energy ( $E_J$ ), zero-order energy ( $E_{0J}$ ) and the partial derivative ( $dE_J/d\xi$ ) in Eq. 3,

$$E_J = E_{0J} + \frac{dE}{d\xi} \Delta \xi \tag{3}$$

the  $\Delta \xi$  value is calculated for each band. The average for the four observed bands is determined. From the average  $\Delta \xi$  value thus determined in the five complexes, the spin-orbit interaction parameter ( $\xi$ ) for  $Pr^{3+}$  in each of the complexes has been calculated using the relation

$$\xi = \xi^0 + \Delta \xi \tag{4}$$

where  $\xi^0$  is aquo ion value of 750 cm<sup>-1</sup>. Eigenvalues and eigenvectors have been evaluated by solving the energy matrices for  $f^2(\Pr^{3+})$ configurations<sup>14</sup> using spectrum 31 micro computer. Observed and calculated energies along with the spin-orbit interaction ( $\xi$ ) parameters are presented in Table 2.

**Table 1** Computed zero-order energies  $(E_{0J})$  and the partial derivatives  $dE_J/d\xi$  for  ${}^{1}D_2$ ,  ${}^{3}P_0$ ,  ${}^{3}P_1$ and  ${}^{3}P_2$  levels in  $f^2$  configuration. ( $E^1 = 4550.39$ ,  $E^2 = 23.83$ ,  $E^3 = 460.26$ )

Term	$E_{0J}  ({\rm cm}^{-1})$	$dE_J/d\xi$
${}^{1}D_{2}$ ${}^{3}P_{0}$ ${}^{3}P_{1}$ ${}^{3}P_{2}$	17264.0 20830.0 21457.0 22711.0	3.02 1.91 3.07 5.28

	Acetylacetonate of praseodymium(III) in									
	МА	<u> </u>	EA		DMF		(MA +	EA)	(MA + DMF	EA) +
Transition from <sup>3</sup> H <sub>4</sub>	Obs.	Cal.	Obs.	Cal.	Obs.	Cal.	Obs.	Cal.	Obs.	Cal.
<sup>1</sup> D <sub>2</sub>	17089	17138	17002	17104	16873	17068	17002	17112	16944	17121
$^{3}\mathbf{P}_{0}^{2}$	20763	20750	20720	20728	20720	20706	20763	20734	20784	20739
<sup>3</sup> P,	21316	21329	21293	21294	21316	21258	21339	21303	21362	21311
$^{3}P_{2}$	22542	22493	22542	22431	22491	22368	22491	22446	22542	22461
σ	±	36	±	75	±	119	±	63	±	103
ξ	708.4 69		6.9 685.1		699.8		742.6			

**Table 2** Observed  $(E_{obs})$  and calculated  $(E_{cal})$  energies  $(cm^{-1})$  of the absorption bands of  $Pr^{3+}$  in acetylacetonate dissolved in different organic solvents.  $(E^1 = 4550.39, E^2 = 23.83, E^3 = 460.26)$ 

 $\sigma$ -R.M.S. Deviation  $\xi$ -Spin orbit parameter

MA: Methyl alcohol, EA: Ethyl alcohol, DMF: Dimethyl formamide.

#### **Spectral Intensities and Radiative Lifetimes**

Measured oscillator strengths (f) of the observed spectral lines of  $Pr^{3+}$ in acetylacetonate in five different organic solvents are presented in Table 3. The equation for the oscillator strength of a transition between the ground state  $(\psi J)$  and an excited state  $(\psi'J')$  of the lanthanide ion is given by Kirby and Palmer<sup>15</sup>

$$f_{\text{expt}} = f_{\text{ed}} = \chi \left[ \frac{8\pi^2 mc}{3h(2J+1)} \right] v \sum_{\lambda=2,4,6} \Omega_{\lambda} (\psi J \| U^{\lambda} \| \psi' J')^2$$
(5)

where  $f_{ed}$  is the electric dipole linestrength of the transition between the ground  $(\psi J)$  and upper  $(\psi' J')$  states,  $\Omega_{\lambda}$  is the Judd-Ofelt parameter,  $\|U^{\lambda}\|$  is the transition matrix element,  $\nu$  is the energy of the band in cm<sup>-1</sup>,  $\chi = (n^2 + 2)^2/9n$  is the Lorentz field factor which is a function of the refractive index of the bulk medium and J is the total angular momentum of the grand level, which for Pr<sup>3+</sup> is 4. The other symbols have their usual significance.  $\|U^{\lambda}\|^2$  values are first calculated for the intermediate coupling scheme.<sup>16</sup> Substituting the appropriate values,

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**Table 3** Measured ( $f_{expl}$ ) and calculated ( $f_{eal}$ ) oscillator strengths (× 10<sup>6</sup>) of the absorption spectral lines of  $Pr^{3+}$  in acetylacetonate dissolved in different organic solvents along with the Judd-Ofelt intensity parameters ( $\Omega_{\lambda}$ ).

	Pr <sup>3+</sup> 8	acetylace	etonate in												
	MA			EA			DMF			<b>MA</b> +	EA		+ W)	- EA) +	DMF
Terms	fexpt	fcai	f ratio w.r.t. <sup>3</sup> P <sub>0</sub>	fexpt	fcal	f ratio w.r.t. <sup>3</sup> P <sub>0</sub>	fexpi	$f_{cal}$	f ratio w.r.t. <sup>3</sup> P <sub>0</sub>	fexpt	fcai	f ratio w.r.t. <sup>3</sup> P <sub>0</sub>	fexpt	fcal	f ratio w.r.t. <sup>3</sup> P <sub>0</sub>
<sup>1</sup> D <sub>2</sub>	0.367 0.103 0.330	0.367 0.214 0.215	3.6 1.0 3.2	0.314 0.093 0.293	0.314 0.191 0.192	3.4 1.0 3.2	0.461 0.246 0.420	0.461 0.330 0.335	1.9 1.0	0.392 0.063 0.270	0.392 0.163 0.166	6.2 1.0 4.3	0.520 0.204 0.422	0.520 0.308 0.311	2.5 1.0 2.1
<sup>3</sup> P <sub>2</sub>	0.969	0.969	9.4	0.781	0.781	8.4	1.313	1.313	5.3	0.687	0.687	10.9	1.547	1.547	7.6
a	ŦI	0.082		Ť	0.070		н Н	.059		)+	0.072		Ŧ	0.076	
Ω2 × 1( Ω4 × 1( × 1(	$y^{20} = 6.0$ $y^{20} = 0.0$ $y^{20} = 2.0$ $y^{20} = 1.0$	675 415 329			7.4 0.36 1.36	53 53 53		0.6 2.8 1.2	55 55 96		16.0 0.3 1.4 1.3	74 13 70 54	ż	6.11 0.48 3.33 1.36	2000

o-R.M.S. Deviation: MA: Methyl alcohol, EA: Ethyl alcohol, DMF: Dimethyl formamide.

four equations were formed for the four bands namely  ${}^{1}D_{2}$ ,  ${}^{3}P_{0}$ ,  ${}^{3}P_{1}$  and  ${}^{3}P_{2}$  as follows:

$$\begin{aligned} f({}^{1}\mathbf{D}_{2}) &= 0.1205 \times 10^{11} \, \nu[\Omega_{2}(0.0026) + \Omega_{4}(0.0170) + \Omega_{6}(0.0520)] \\ f({}^{3}\mathbf{P}_{0}) &= 0.1205 \times 10^{11} \, \nu[\Omega_{2}(0) + \Omega_{4}(0.1728) + \Omega_{6}(0)] \\ f({}^{3}\mathbf{P}_{1}) &= 0.1205 \times 10^{11} \, \nu[\Omega_{2}(0) + \Omega_{4}(0.1707) + \Omega_{6}(0)] \\ f({}^{3}\mathbf{P}_{2}) &= 0.1205 \times 10^{11} \, \nu[\Omega_{2}(0) + \Omega_{4}(0.0362) + \Omega_{6}(0)] \end{aligned}$$

The three phenomenological parameters  $\Omega_2$ ,  $\Omega_4$  and  $\Omega_6$  were evaluated by the least squares fit analysis and are presented in Table 3, along with the calculated oscillator strengths. Small r.m.s. deviations support the applications of Judd-Ofelt theory.<sup>17,18</sup>

Electric dipole linestrengths  $(S_{ed})$ , magnetic dipole linestrengths  $(S_{md})$ , radiative transition probabilities  $A(\psi J)$ , radiative lifetimes  $(T_R)$  and the branching ratios  $(\beta_R)$  have been theoretically evaluated using the procedure followed by Lakshman and Rama Moorthy.<sup>19</sup> Radiative lifetimes and the branching ratios thus evaluated for the excited  ${}^{3}P_{0}$ ,  ${}^{3}P_{1}$  and  ${}^{1}D_{2}$  levels of  $Pr^{3+}$  in acetylacetonate chelate in different solvents are presented in Tables 4 and 5 respectively.

#### DISCUSSION

From Table 3, it can be noted that the intensities of the observed spectral lines are slightly increased in DMF and MA + EA + DMF solvents compared to other organic solvents and the intensity ratios of  ${}^{1}D_{2}$ ,  ${}^{3}P_{1}$  and  ${}^{3}P_{2}$  w.r.t.  ${}^{3}P_{0}$  are high in MA, EA and (MA + EA) and low in DMF and MA + EA + DMF solvents. The order of the three phenomenological parameters  $\Omega_{2}$ ,  $\Omega_{4}$  and  $\Omega_{6}$  derived from the oscillator strengths applying J-O theory are  $\Omega_{2} > \Omega_{6} > \Omega_{4}$  in all the five chelate complexes studied. The theoretically estimated radiative lifetimes ( $T_{R}$ ) of the  ${}^{3}P_{1}$ ,  ${}^{3}P_{0}$  and  ${}^{1}D_{2}$  levels of  $Pr^{3+}$  in acetylacetonate in five organic solvents are in the following order (Table 4).

 ${}^{3}P_{1}(T_{R}): MA > EA > (MA + EA) + DMF) > DMF > MA + EA$  ${}^{3}P_{0}(T_{R}): MA > (MA + EA) + DMF) > EA > DMF > MA + EA$  ${}^{1}D_{2}(T_{R}): MA > (MA + EA) + DMF) > EA > DMF > MA + EA$ 

Usually the branching ratios are high for potential laser transitions.<sup>20</sup> It is therefore predicted from Table 5 that the transitions  ${}^{3}P_{1} \rightarrow {}^{3}F_{3}$ ,  ${}^{3}P_{0} \rightarrow {}^{3}F_{2}$  and  ${}^{1}D_{2} \rightarrow {}^{3}F_{4}$  which have high ( $\beta_{R}$ ) values are the most potential laser transitions.

**Table 4** Radiative lifetimes  $(T_R)$  for the excited  ${}^{3}P_1$ ,  ${}^{3}P_0$  and  ${}^{1}D_2$  levels of  $Pr^{3+}$  in acetylacetonate in five organic solvents.

States	$MA T_R (\mu \text{ sec})$	EA $T_R$ ( $\mu$ sec)	DMF $T_R$ ( $\mu$ sec)	$MA + EA T_R (\mu \text{ sec})$	$\frac{MA + EA + DMF}{T_R (\mu \text{ sec})}$
<sup>3</sup> P,	79	67	58	34	63
<sup>3</sup> P <sub>0</sub>	70	62	55	31	64
${}^{1}D_{2}^{0}$	413	362	340	178	393

**Table 5** Theoretically computed branching ratios ( $\beta_R$ ) for the excited flourescent levels of  $Pr^{3+}$  in acetylacetonate in different organic solvents.

SLJ	S'L'J'	$MA_{\beta_R}$	$\frac{\mathbf{E}\mathbf{A}}{\boldsymbol{\beta}_{\boldsymbol{R}}}$	$DMF \\ \beta_R$	MA + EA $\beta_R$	(MA + EA) + DMF $\beta_R$
(1)	(2)	(3)	(4)	(5)	(6)	(7)
<sup>3</sup> P <sub>1</sub>	<sup>1</sup> D <sub>2</sub>	0.001	0.001	0.001	0.002	0.001
-	${}^{1}G_{4}$	0.004	0.003	0.007	0.001	0.004
	<sup>3</sup> F <sub>4</sub>	0.013	0.010	0.014	0.004	0.013
	<sup>3</sup> F <sub>3</sub>	0.542	0.552	0.507	0.584	0.502
	${}^{3}F_{2}$	0.324	0.330	0.300	0.353	0.257
	${}^{3}H_{6}$	0.054	0.027	0.052	0.017	0.074
	<sup>3</sup> H <sub>5</sub>	0.034	0.055	0.089	0.029	0.120
	<sup>3</sup> H <sub>4</sub> .	0.028	0.022	0.030	0.009	0.028
${}^{3}P_{0}$	$^{1}D_{2}$	0	0	0	0	0
	${}^{1}G_{4}$	0.005	0.004	0.006	0.002	0.006
	<sup>3</sup> F <sub>4</sub>	0.012	0.010	0.014	0.004	0.014
	${}^{3}F_{2}$	0.838	0.889	0.824	0.944	0.780
	$^{3}H_{6}$	0.076	0.040	0.077	0.025	0.159
	<sup>3</sup> H₄	0.069	0.056	0.079	0.024	0.081
<sup>1</sup> D <sub>2</sub>	${}^{1}G_{4}$	0.103	0.109	0.116	0.108	0.093
-	<sup>3</sup> F₄	0.727	0.760	0.738	0.783	0.697
	<sup>3</sup> F <sub>3</sub>	0.036	0.036	0.036	0.037	0.035
	${}^{3}F_{2}$	0.028	0.026	0.028	0.024	0.028
	<sup>3</sup> H <sub>6</sub>	0.011	0.008	0.012	0.002	0.010
	³Н,	0	0	0	0	0
	<sup>3</sup> H <sub>4</sub>	0.060	0.060	0.045	0.045	0.136

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